

Chapter 5 Conclusions and further research

In this dissertation, we have examined the concept of programmable cellular logic arrays at several different levels. A number of examples have been given to demonstrate the feasibility of PL specifically. Several of these examples have been shown to be superior in important ways to more conventional versions. More importantly, however, we have also discussed PL in more abstract terms in an attempt to contribute some understanding and coherence which will be more useful than specific examples to following researchers in this field.

In order to attach a more global meaning to research of this kind, the work must be viewed in the larger context of systems design. From this vantage point, it may be said that the principal tenet underlying this work is that of maximizing design congruence. The property of congruence is used here to refer to the match, fit, and consistency of a design with its environment. This dissertation has attempted to improve several congruence relationships inherent in the design of digital computer hardware through the use of programmable cellular logic.

One such relationship is that which exists between a design and the technology available for physically realizing that design. We have discussed large-scale integrated circuit technology and have shown several ways in which programmable logic arrays can potentially provide better utilization of LSI technology than other cellular forms. In particular, PL offers a

new solution to the customization problem, facilitates testing, and improves failure tolerance and repairability.

As a contribution to a better understanding of cellular arrays in general, we have presented several characteristics of arrays which may be viewed as the dimensions of an n-space of all cellular arrays. It is felt that previous research in this area has too often concentrated only on specific array designs (isolated points in the space) without relating to other arrays or attempting a real understanding of the design. Therefore, we have discussed a number of ways in which arrays may be compared, contrasted, and related.

Another congruence relationship of interest is that which exists between a design and the set of tasks it is intended to perform. It is asserted that generality (i.e. the power, scope, and range of functions performed; opposite to specificity) is a very important characteristic in the systems design process. The degree of generality required to synthesize a given set of functions affects the design of a machine to perform those functions in fundamental and important ways. In addition, we may use the dimension of generality to order and relate various functions and machines. In this work, we have ordered the discussion of PL arrays into two broad areas -- low generality and high generality. Via several examples, we have been able to demonstrate the feasibility of PL in both areas.

We began by presenting two slightly different versions of

an array intended to perform the simple arithmetic and parity functions. Despite the high similarity between the two cells, one array was seen to be more efficient at performing the arithmetic functions, while the other was superior on the parity functions. This simple example demonstrates how small changes in an array can be used to adjust the array's efficiency over the target set of functions. This result is made stronger by noting that, because of the specificity of their functions, low-g arrays are inherently less "tunable" than other arrays.

A significantly different low-g example is the shift register array S1. Each cell in this array contains an n-bit shift register and connections to the four nearest-neighbor cells. An expression was derived which gives the optimal value of n as a function of the expected manufacturing yield over the array. We have shown how this array design may be used to achieve significantly better utilization of LSI technology than the discretionary wiring or 100-percent-yield processes in the task of creating shift registers in the presence of numerous manufacturing defects. This example demonstrates congruence both to its task and to its physical implementation.

We began the discussion of the high-generality area with the presentation of a cell schema for high-g arrays. The principal new idea here (in addition to the fact that cell forms are nearly non-existent in the literature) is that the cell function takes its inputs from the outputs of the cell connection function, rather than from the inputs to the cell. A number of

properties fundamental to the efficient application of PL arrays to high-g problems were also discussed and related to this cell schema.

Several new techniques have been developed which can improve the congruence between an array and the function it realizes. One such technique involves a scheme for adjusting the angle at which signal buses traverse a rectangular array of cells in order to provide a suitable range of fan-in and fan-out on these signals. This new idea has applicability over a wide range of cellular array types.

Some results have been derived concerning the usefulness of various 3-variable functions in synthesizing arbitrary combinatorial functions. A group of transformations consistent with PL array synthesis was introduced. It includes input permutation, negation, and duplication and output inversion. Under these transformations, it was shown that only 10 functions are necessary to generate all 256 3-variable functions. Several of these 10 functions are each capable of generating nearly 1/3 of all 3-variable functions. It is suggested that these same functions are more efficient than other 3-variable functions when used to synthesize arbitrary combinatorial functions under the same transformations. Several functions often proposed as primitives for this task (e.g., majority gate and XOR) were shown to be the weakest of all 3-variable functions in this comparison.

As an application of high-g PL arrays, we have discussed

the problem of control in digital computers. A PL control array was presented as an alternative to the conventional microprogramming approach. Potential advantages of the PL control array over microprogrammed control include greater flexibility and parallelism, improved failure tolerance and diagnosability, and elimination of irregular (non-iterative) logic. It was also shown that, for all machines above a certain (small) size, the total number of components required with PL control is less than that with current microprogramming techniques. Control for a small computer was implemented in detail using a PL array.

A number of interesting research problems have been suggested by this work. The most obvious one is the development of algorithms for automatic programming of PL arrays. This may be approached in several ways. One type of algorithm necessary is that which assigns states and paths, etc., to build up a given structure in an unprogrammed array. Another type of algorithm is that which concentrates on correcting spontaneous defects in the array by making very local perturbations in the array.

Although the arrays proposed in this work are largely within the scope of present LSI technology, some research in this area would be appropriate. PL often requires more complex connections between circuit layers and/or more layers than conventional LSI. In order to actually build these devices, a more thorough knowledge of the added costs of connections,

layers, slanted buses, etc., should be obtained. Also, an important possibility to be investigated is that of using slow-write fast-read control elements in the parameter part of the PL cell.

Our discussions of the usefulness of 3-variable functions under certain transformations logically deserves extension. Given a set of transformations of cell inputs and outputs, what primitive or set of primitives are most effective in synthesizing all n -variable functions for a given n ? How does one find these primitives? Another possibility is to weight each of the object classes of functions according to its desirability. Then the question becomes one of optimizing the "fit" of the class generated by the primitives to the object class.

Another theoretical consideration is that of testing PL arrays. How does the flexibility of the interconnection function affect the effectiveness of various testing procedures? What algorithms are most efficient in testing an array with a given connection topology and expected yield?

The most logical specific extension of this work has to do with the combinatorial functions discussed in Section 4.4.1. The effectiveness of imbedding several of these 3-variable functions (perhaps in combination) into a complete high-g cell should be investigated. Comparisons should be made between an array of these cells and conventional methods (as well as other cellular forms). This would also serve to further substantiate

the applicability of the high-q cell schema which was presented.

Another specific problem concerns the shift register array S1. How does the fault-avoidance capability of this array vary with increasingly complex connection structures? What is the optimal connection function for a given range of defect densities? Solutions to these problems would have implications for fault-avoidance in other more general arrays as well.

It remains to be seen whether the computer science community and/or the commercial manufacturers will take up the banner of PL. Hopefully, this dissertation has provided significant justification for further interest in this technique.

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13. ABSTRACT In recent years, technological advances have provided the designer of computing hardware with the ability to batch-fabricate large numbers of logic components on a single semiconductor slice. Numerous researchers have investigated the synthesis of various kinds of digital logic by using arrays of identical cells. This dissertation considers cellular arrays whose individual cell functions are determined by parameter flip-flops and logic gates in the cell, rather than by a physical customizing operation during manufacture. Potential advantages of this technique include functional variability after manufacture, more efficient testing, and enhanced failure tolerance. Arrays may be classified according to their generality, i.e., the number and range of the tasks which they are designed to perform. Two significantly different examples of low-generality arrays are presented and analyzed. One, a shift register array, is shown to be more effective than some conventional techniques for creating shift registers in the presence of numerous manufacturing defects. A new cell schema is introduced which exhibits properties important in the synthesis of high-generality functions. Techniques are presented for improving the match between an array design and the target class of tasks. As an example, the problem of central processor control logic is approached in terms of a programmable logic array. A small computer is implemented in detail using these techniques. This method of synthesizing control is compared to a more conventional microprogramming approach.			

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